

Logarithmic Functions are inverse functions of an exponential function thus $f(x) = b^x$ and $g(x) = \log_b(x)$

Evaluate each expression

1) $\log_{10} 1000$

2) $\log_9 27$

3) $\log_{16} \left(\frac{1}{8}\right)$

$$x = (b)^y$$

$$f^{-1}(x) = \log_b(x)$$

Note: $b > 0$ and $b \neq 1$

- They are continuous functions over $(0, \infty)$
- They are One – to – One Functions
- Domain: $(0, \infty)$ All real Numbers greater than Zero
- Range: $(-\infty, \infty)$ All Real Numbers
- Increasing function if $b > 1$
- Decreasing function if $0 < b < 1$
- As $x \rightarrow 0^+$ the y-axis is a vertical asymptote for the graph of the function.
- The graph of the function has an x-intercept: $(1, 0)$
- The graph of the function does not have a y-intercept.

Key points of the graph also include: $(b, 1)$ & $\left(\frac{1}{b}, -1\right)$

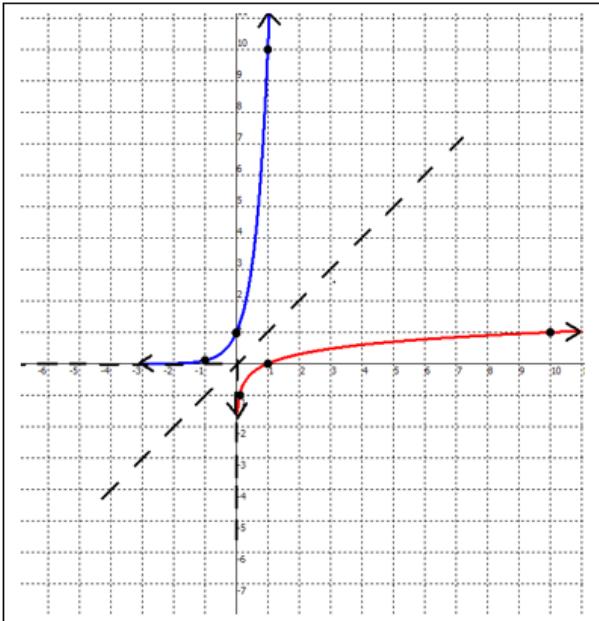
$$g(x) = 10^x$$

$$g^{-1}(x) = \log_{10}(x) \quad g^{-1}(x) = \log(x)$$

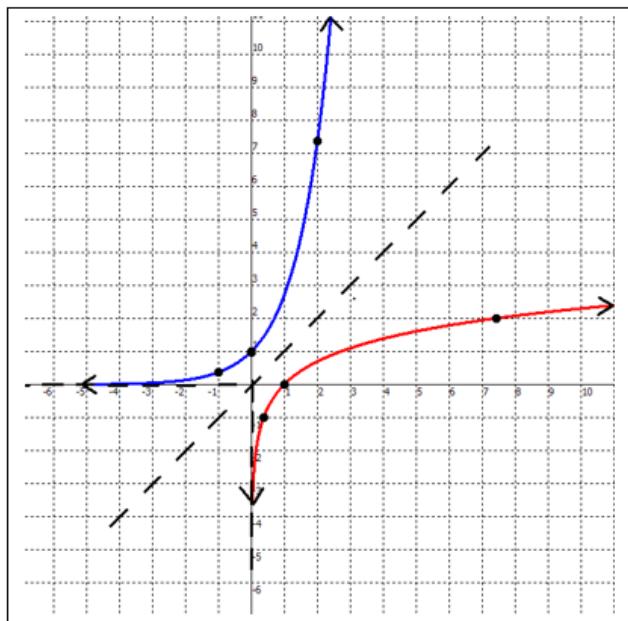
$$g(x) = e^x$$

$$g^{-1}(x) = \log_e(x) \quad g^{-1}(x) = \ln(x)$$

Common Logarithm Function



Natural Logarithm Function



$$y = \log_b(x)$$

x	y
$\frac{1}{b^2}$	-2
$\frac{1}{b}$	-1
1	0
b	1
b^2	2

$x=0$ Asym

$$y = \log_2(x)$$

x	y
$\frac{1}{4}$	-2
$\frac{1}{2}$	-1
1	0
2	1
4	2

$x=0$ Asym

$$y = \log_{10}(x) = \log(x)$$

x	y
$\frac{1}{100}$	-2
$\frac{1}{10}$	-1
1	0
10	1
100	2

$x=0$ Asym

$$y = \log_e(x) = \ln(x)$$

x	y
$\approx \frac{1}{7.4}$	-2
$\approx \frac{1}{2.7}$	-1
≈ 1	0
≈ 2.7	1
≈ 7.4	2

$x=0$ Asym

$$y = \log_{\frac{1}{2}}(x)$$

x	y
4	-2
2	-1
1	0
$\frac{1}{2}$	1
$\frac{1}{4}$	2

$x=0$ Asym

$$y = \log_{\frac{1}{3}}(x)$$

x	y
9	-2
3	-1
1	0
$\frac{1}{3}$	1
$\frac{1}{9}$	2

$x=0$ Asym

$$y = \log_{\frac{3}{4}}(x)$$

x	y
$\frac{16}{9}$	-2
$\frac{4}{3}$	-1
1	0
$\frac{3}{4}$	1
$\frac{9}{16}$	2

$x=0$ Asym

$$y = a \cdot \log_b(x+n) + m$$

$-n$	$\frac{x}{b^2}$	$\cdot a$	$+ m$
	$\frac{1}{b^2}$	-2	
	$\frac{1}{b}$	-1	
	1	0	
	b	1	
	b^2	2	

$x=0$ Asymptote

$$y = \log_{\frac{1}{2}}(x-3)-6$$

$+3$	$\frac{x}{b^2}$	-6
7	4	-2
5	2	-1
4	1	0
$3\frac{1}{2}$	$\frac{1}{2}$	1
$3\frac{1}{4}$	$\frac{1}{4}$	2

$x=3 \leftarrow x=0$ Asymptote

