

The scalar quantity of the magnitude of the force  $\mathbf{F}$  in the direction of vector  $\mathbf{v}$  is:

The dot product  $\mathbf{u} \cdot \mathbf{v}$  of vectors  $\mathbf{u} = \langle u_1, u_2, u_3 \rangle$  and  $\mathbf{v} = \langle v_1, v_2, v_3 \rangle$  is the scalar

The angle between two nonzero vectors  $\mathbf{u}$  and  $\mathbf{v}$ :

Perpendicular or orthogonal vectors

Properties of dot products: If  $\mathbf{u}$ ,  $\mathbf{v}$  and  $\mathbf{w}$  are any vectors and  $c$  is a scalar, then:

Projecting one vector  $\mathbf{u}$  on to another vector  $\mathbf{v}$

If  $\mathbf{u}$  represents a force then  $\text{proj}_{\mathbf{v}}\mathbf{u}$  (the vector projection of  $\mathbf{u}$  on  $\mathbf{v}$ ) represents the effective force in the direction of  $\mathbf{v}$ .

The vector projection of  $\mathbf{u}$  on to  $\mathbf{v}$

Both vector projection of  $\mathbf{u}$  on to  $\mathbf{v}$  and the scalar component of  $\mathbf{u}$  on to  $\mathbf{v}$  depend only on the direction of the vector  $\mathbf{v}$  and not its length (because we dot  $\mathbf{u}$  with  $\frac{\mathbf{v}}{|\mathbf{v}|}$ , which is the direction of  $\mathbf{v}$ ).