

Substitution with Trigonometry

3 basic trig substitutions

$$\sqrt{a^2 + x^2} =$$

$$x = a \sin x$$

$$x = a \sec \theta$$

$$\int \frac{3dy}{\sqrt{1+9y^2}}$$

$$\int \sqrt{1-9t^2} dt$$

$$\int \frac{5dx}{\sqrt{25x^2-9}}, x > \frac{3}{5}$$

$$\int \frac{dx}{x^2 \sqrt{x^2 + 1}}$$

$$\int_1^e \frac{dy}{y \sqrt{1 + (\ln y)^2}}$$

$$(x^2 + 1)^2 \frac{dy}{dx} = \sqrt{x^2 + 1}, y(0) = 1$$