

Sequences

An infinite sequence of numbers is a function whose domain is the set of positive integers

The sequence  $\{a_n\}$

If no such number  $L$  exists,

If  $\{a_n\}$  converges to  $L$  we write

The sequence  $\{\sqrt{n}\}$

The sequence  $\{a_n\}$  diverges to infinity if

Let  $\{a_n\}$  and  $\{b_n\}$  be sequences of real numbers and let  $A$  and  $B$  be real numbers. The following rules hold if

Sum Rule

Quotient Rule

Difference Rule

Product Rule

Constant Multiple Rule

## The sandwich theorem for sequences

If  $|b_n| \leq c_n$  and  $c_n \rightarrow 0$  then  $b_n \rightarrow 0$

$$\lim_{n \rightarrow \infty} \frac{1}{n} = 0$$

$$\lim_{n \rightarrow \infty} K = K$$

$$\lim_{n \rightarrow \infty} (-1)^{n+1}$$

$$\lim_{n \rightarrow \infty} \frac{\cos n}{n} = 0$$

$$\lim_{n \rightarrow \infty} \frac{1}{2^n} =$$

$$\lim_{n \rightarrow \infty} (-1)^n \left( \frac{1}{n} \right) = 0$$

$$\lim_{n \rightarrow \infty} \sqrt{\frac{n+1}{n}} =$$

$$\lim_{n \rightarrow \infty} \frac{\ln n}{n} =$$

$$\lim_{n \rightarrow \infty} \frac{2^n}{5n} =$$

$$\lim_{n \rightarrow \infty} \sqrt[n]{n} =$$

$$\lim_{n \rightarrow \infty} x^{\frac{1}{n}} = 1$$

$$\lim_{n \rightarrow \infty} x^n = 0$$

$$\lim_{n \rightarrow \infty} \left( 1 + \frac{x}{n} \right)^n = e^x$$

$$\lim_{n \rightarrow \infty} \frac{x^n}{n!} = 0$$

$$\text{Ex } a_n = \frac{1}{n!}$$

$$1, -\frac{1}{4}, \frac{1}{9}, -\frac{1}{16}, \frac{1}{25}, \dots$$

$$a_1 = 2 \quad a_2 = 1 \quad a_{n+2} = \frac{a_{n+1}}{a_n}$$

$$a_n = \frac{n + (-1)^n}{n}$$

$$a_n = (-1)^n \left(1 - \frac{1}{n}\right)$$

$$a_n = \frac{\sin^2 n}{2^n}$$